

Joint Workshop: MathSEE-KCETA

Numerical methods for High Performance Computing

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Fixed Point Numerics for Exascale (FiNE)



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Outline

- The HPC landscape
- Ginkgo - A high performance numerical linear algebra library.
- Application 1: MFEM
- Application 2: OpenFOAM
- Application 3: Combustion simulations with PeleLM
- Application 4: Fusion plasma simulations with XGC.
- Conclusions.

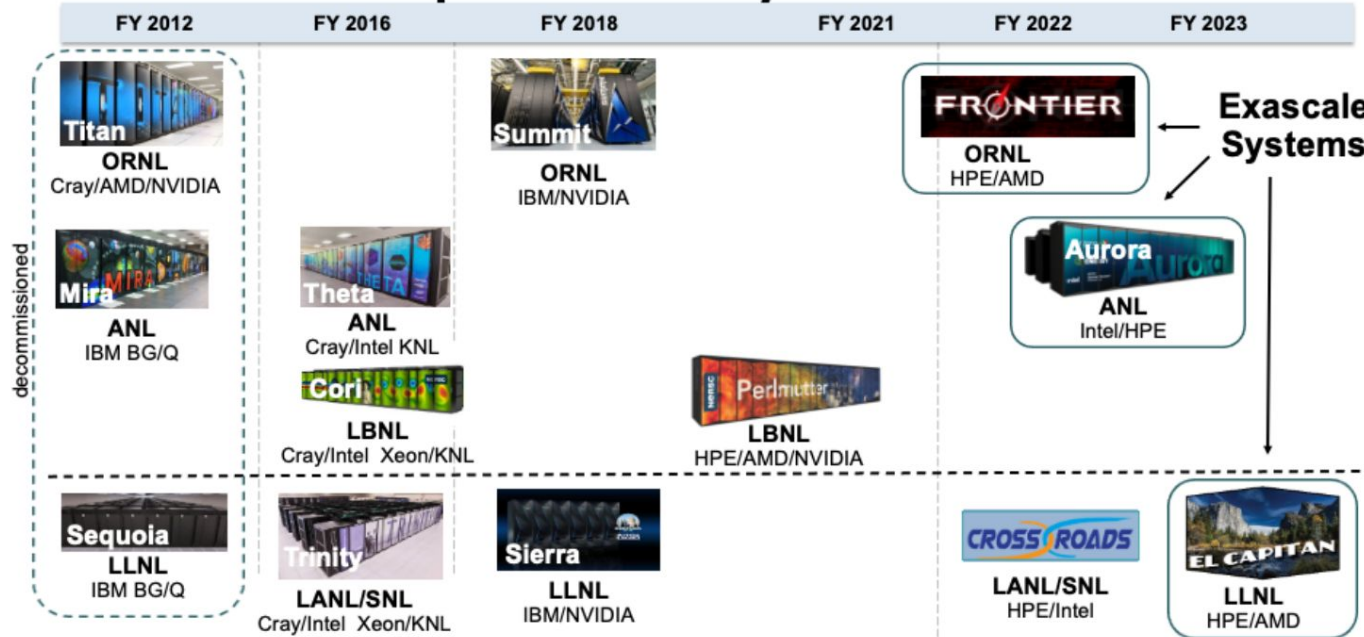
The High Performance Computing (HPC) Landscape

- A first exascale system, Frontier (1.1 EFlops).
- European system in top 3, LUMI with 151 PFlops.
- All systems aiming for efficiency use some form of accelerators.

Rank	System	Cores	Rmax (PFlop/s)	Rpeak (PFlop/s)	Power (kW)
1	Frontier - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE DOE/SC/Oak Ridge National Laboratory United States	8,730,112	1,102.00	1,685.65	21,100
2	Supercomputer Fugaku - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D, Fujitsu RIKEN Center for Computational Science Japan	7,630,848	442.01	537.21	29,899
3	LUMI - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE EuroHPC/CSC Finland	1,110,144	151.90	214.35	2,942
4	Summit - IBM Power System AC922, IBM POWER9 22C 3.07GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM DOE/SC/Oak Ridge National Laboratory United States	2,414,592	148.60	200.79	10,096
5	Sierra - IBM Power System AC922, IBM POWER9 22C 3.1GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM / NVIDIA / Mellanox DOE/NNSA/LLNL United States	1,572,480	94.64	125.71	7,438

The High Performance Computing (HPC) Landscape

DOE HPC Roadmap to Exascale Systems

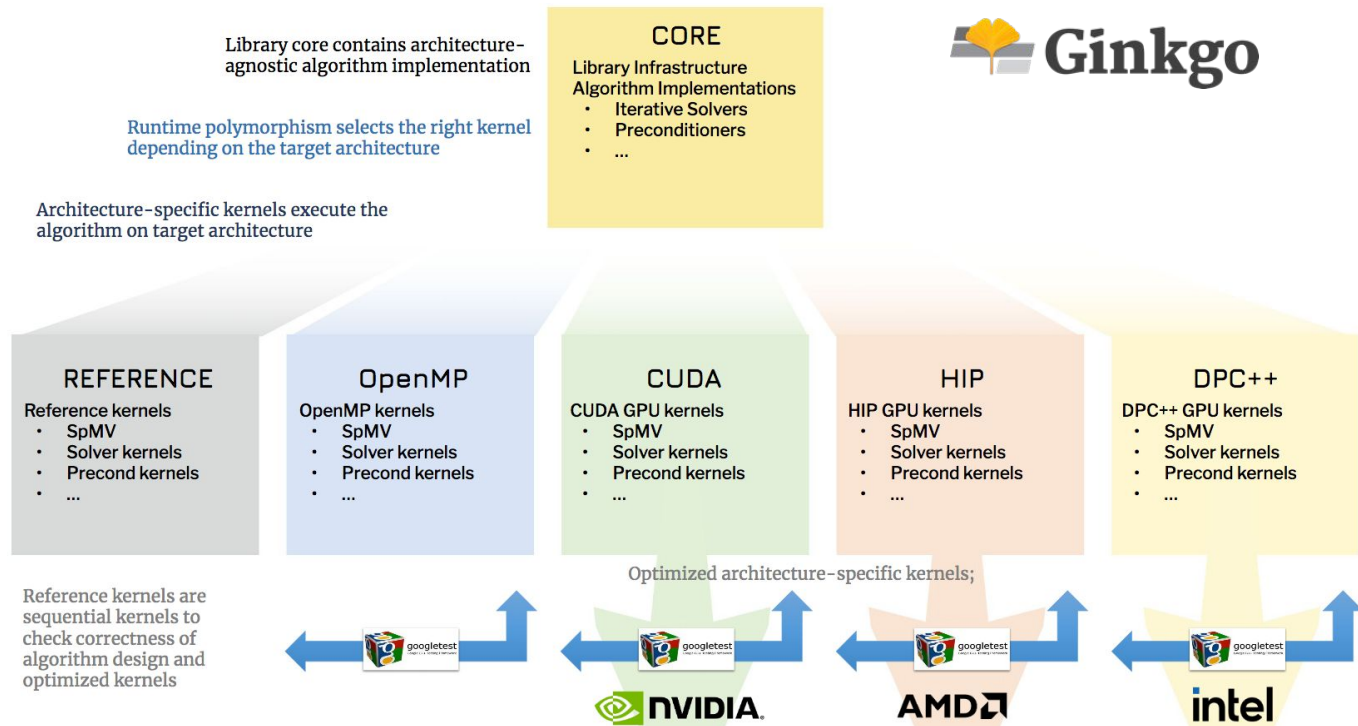


What is the performance distribution ? (GPUs v/s CPUs)

- Consider 1 node of Summit (6 GPUs and 2 sockets of IBM Power 9 with a total of 44 cores)
- Peak Flop of 6 V100 GPU is 40 TFlops. Peak Flop of 2 sockets of IBM Power 9 CPUs is 0.9 TFlops.
- **98%** of the performance on a node is in the GPUs. **Extremely critical** to design implementations and algorithms that work well on GPUs and multi-GPUs.

The Ginkgo software library.

- Focus on high performance sparse linear algebra.
- Thoroughly tested and benchmarked.
- Linear solvers, matrix formats, preconditioners and more.
- Support for multiple backends: CUDA, HIP, DPC++ and OpenMP.



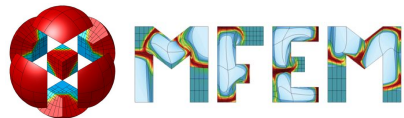
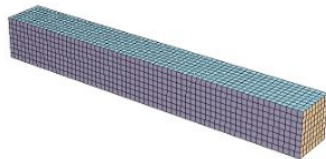
Ginkgo: Current features

	Functionality	OMP	CUDA	HIP	DPC++					
Basic	SpMV	✓	✓	✓	✓	} Thread-to-nonzero, subwarp-to-row, or thread-to-row mapping	Local parallelization strategy	} Local algorithmic approach		
	SpMM	✓	✓	✓	✓				} subwarp-to-row mapping	} Mixed precision support
	SpGeMM	✓	✓	✓	✓					
Krylov solvers	BiCG	✓	✓	✓	✓	} Thread-to-row mapping	} Merged kernels			
	BiCGSTAB	✓	✓	✓	✓					
	CG	✓	✓	✓	✓					
	CGS	✓	✓	✓	✓					
	GMRES	✓	✓	✓	✓					
	IDR	✓	✓	✓	✓					
Preconditioners	(Block-)Jacobi	✓	✓	✓		} subwarp to blocks	} Advanced Mixed precision support			
	ILU/IC		✓	✓		} Subwarp-to-row mapping				
	Parallel ILU/IC	✓	✓	✓		} Thread-to-nonzero mapping				
	Parallel ILUT/ICT	✓	✓	✓		} Subwarp to row mapping		} Asynchronous Fix-point based		
	Sparse Approximate Inverse	✓	✓	✓						
	Algebraic Multigrid	✓	✓	✓		} Composes of other routines				
Batched	Batched BiCGSTAB	✓	✓	✓		} Thread-block to problem mapping	} kernel-inlining & single-kernel design to avoid global memory accesses			
	Batched CG	✓	✓	✓						
	Batched GMRES		✓	✓						

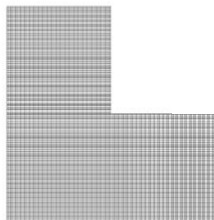
Single GPU applications

Application 1: MFEM: Poisson equation

$$-\Delta u = 1$$

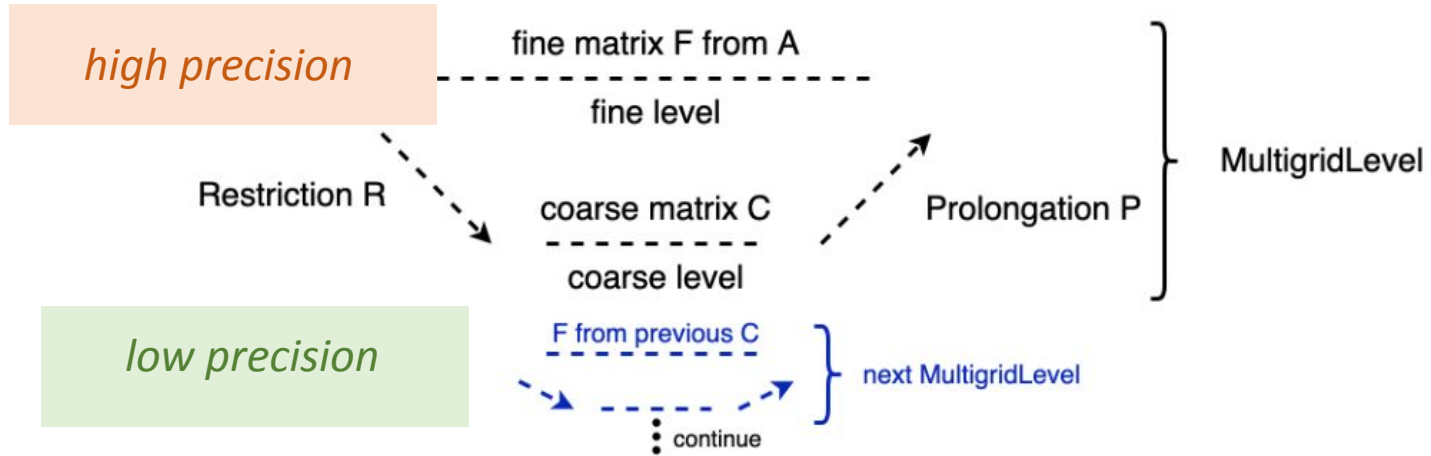


matrices in MFEM
integration test

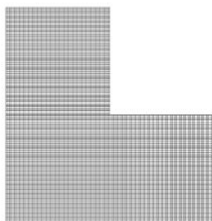
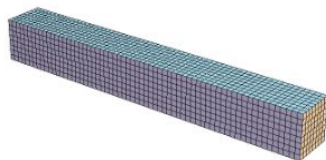


problem	size	nonzero elements
beam (-o2 -l3)	37,281	21,67,425
beam (-o3 -l3)*	120,625	14,070,001
beam (-o4 -l3)	279,873	57,251,713
beam (-o3 -l4)	924,385	111,573,601
L-shape (-o3 -l7)*	443,905	11,066,881
L-shape (-o3 -l8)	1,772,545	44,252,161
L-shape (-o4 -l7)	788,481	28,323,841
L-shape (-o4 -l8)	3,149,825	113,270,785

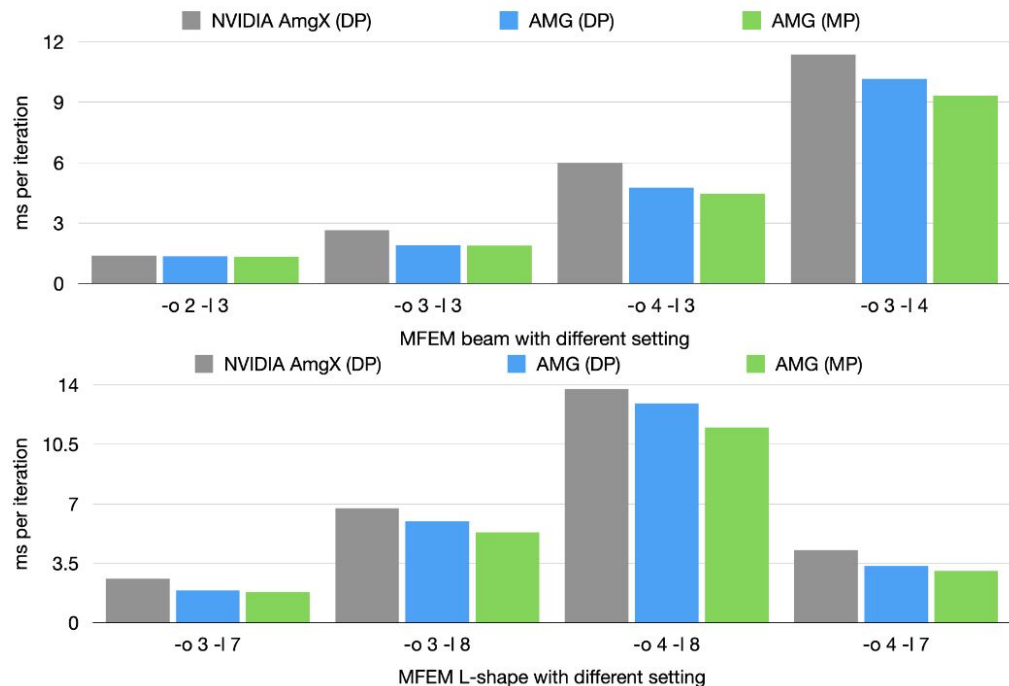
Application 1: MFEM, Multigrid and mixed precision



Application 1: MFEM, Multigrid and mixed precision

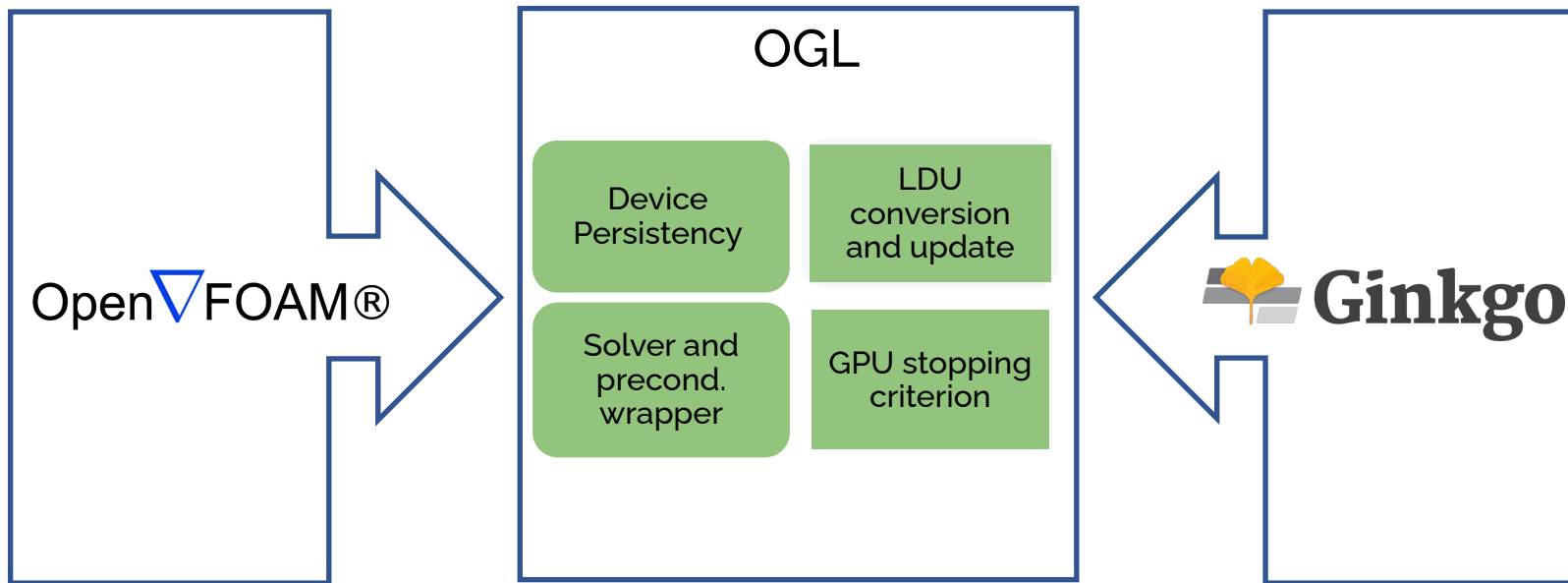


geometry	problem	NVIDIA AmgX (DP)		GINKGO AMG (DP)		GINKGO AMG (MP)	
		runtime [ms]	#iter	runtime [ms]	#iter	runtime [ms]	#iter
Beam	-o 2 -l 3	20.71	15	20.27	15	19.96	15
	-o 3 -l 3	52.94	20	39.93	21	39.56	21
	-o 4 -l 3	155.47	26	128.69	27	120.41	27
	-o 3 -l 4	329.68	29	294.68	29	270.39	29
L-shape	-o 3 -l 7	242.27	93	178.02	93	170.08	94
	-o 3 -l 8	1211.38	180	1033.96	173	943.27	177
	-o 4 -l 8	3452.91	251	3044.24	236	2722.63	237
	-o 4 -l 7	551.99	129	407.27	122	366.99	120



Application 2: OpenFOAM

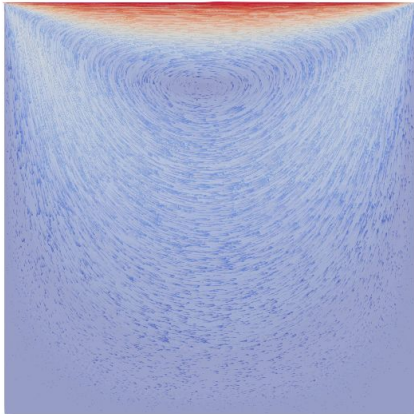
$$\text{Open}\nabla\text{FOAM}^{\text{®}} + \text{Ginkgo} = \text{OGL}^1$$



¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

Application 2.1 : OpenFOAM (Lid driven cavity)

OpenFOAM® +  Ginkgo = OGL¹

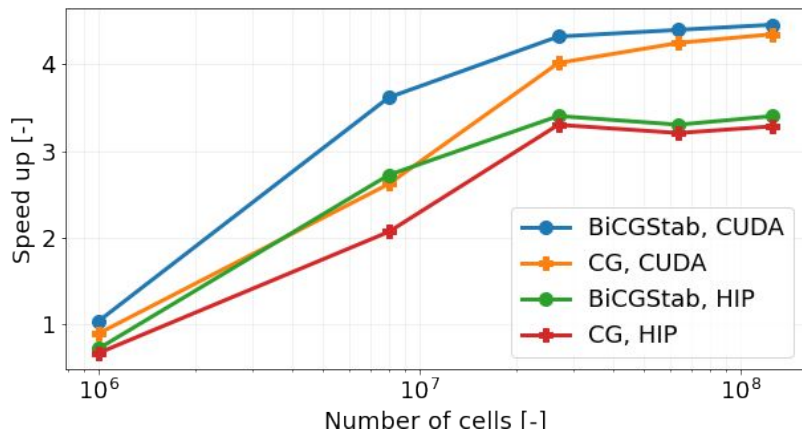


DoFs	1e6 to 25e6
Application	icoFoam
Solver, p	CG, DIC
Solver, U	BiCGStab, DILU

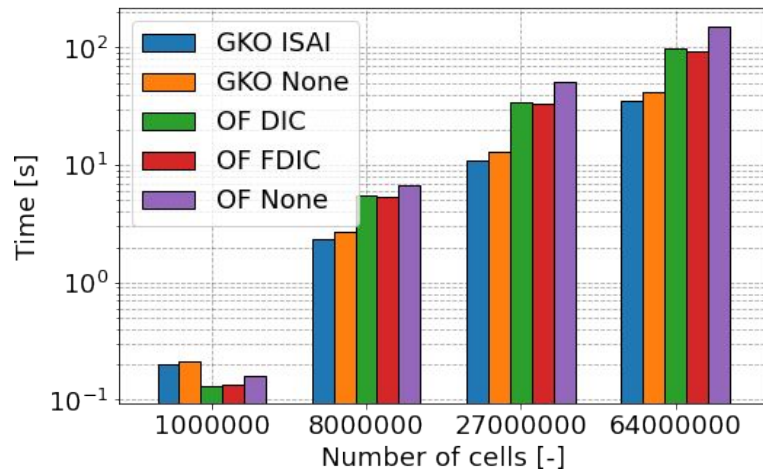
¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

Application 2.1 : OpenFOAM (Lid driven cavity)

OpenFOAM® +  Ginkgo = OGL¹



Single GPU speedup (HIP (MI100) and CUDA (V100)) over CPUs, AMD (32 cores and Intel (76 cores) resp.



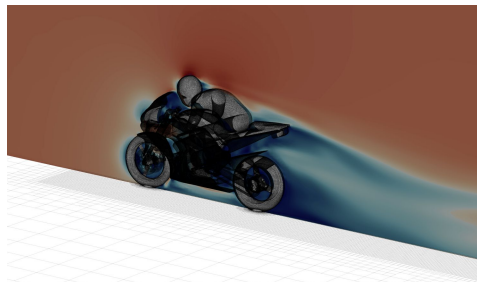
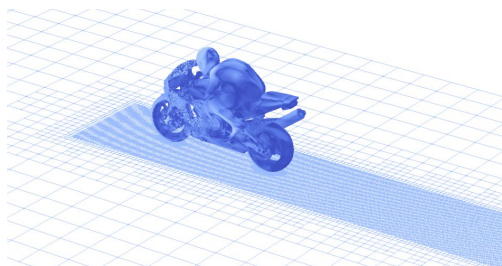
Poisson solver times with different preconditioners (AMD MI100 and AMD CPU, 32 ranks)

¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

Multi-GPU and distributed

Application 2.2 : OpenFOAM (Motorcycle)

OpenFOAM® +  Ginkgo = OGL¹



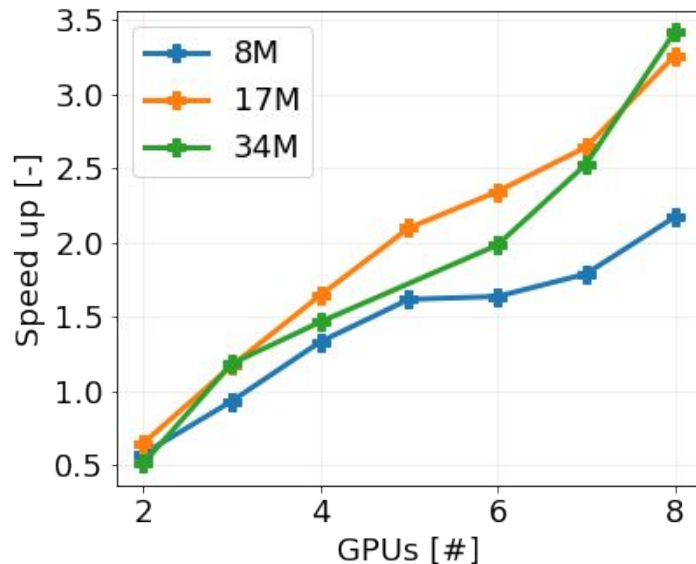
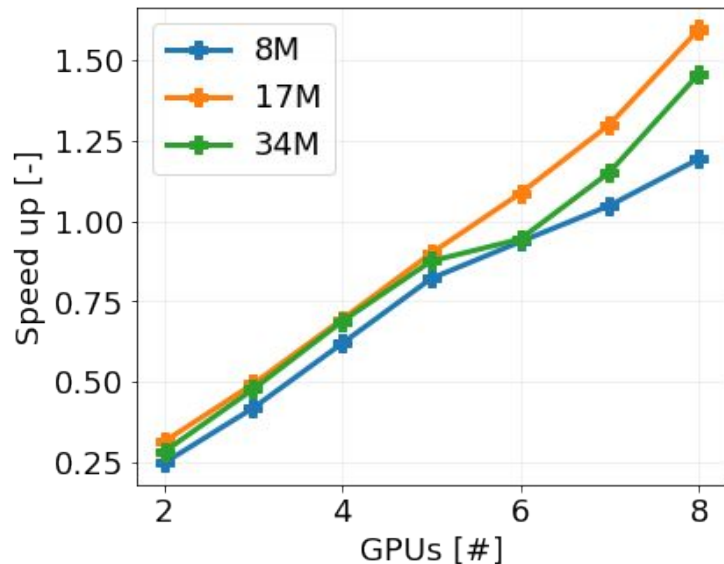
DoF	n*8.678M
Application	simpleFoam
Outer iterations	500
Solver, p	CG
Solver, U	BiCGStab

Case	DoFs
Small	8.678M
Medium	17.356M
Large	26.034M

¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

Application 2.2 : OpenFOAM (Motorcycle)

OpenFOAM® +  Ginkgo = OGL¹



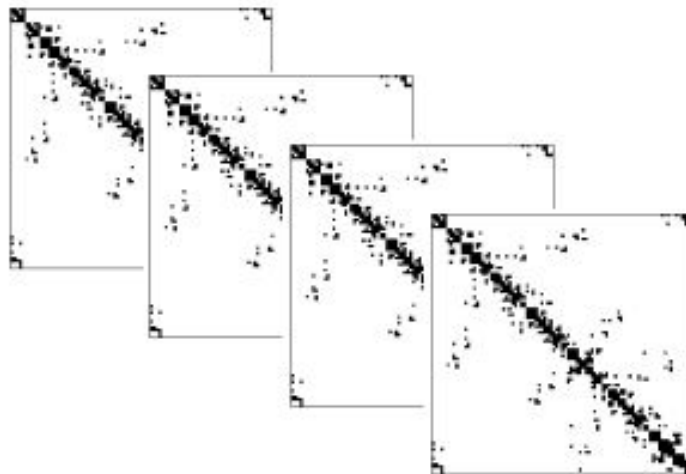
CG speedup with distributed Schwarz preconditioner with ISAI (left), and Multigrid (right) on MI100s versus 32 MPI ranks on an AMD EPYC 7302 with an IC preconditioner.

¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

Batched methods

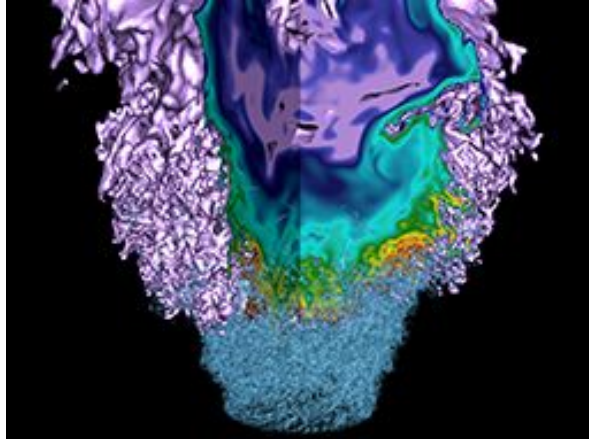
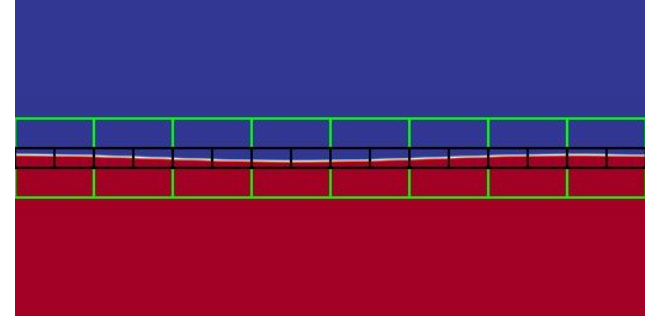
Batched solvers in Ginkgo

- Batching: Independent computations that can be scheduled in parallel.
- Are highly suitable for GPUs and processors with many parallel computing units.
- Can maximize utilization of the GPU, due to excellent scalability.



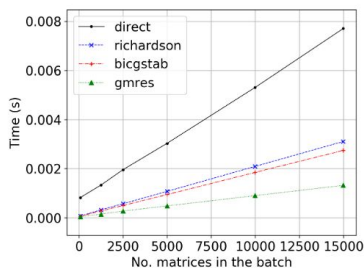
Application 3: Combustion simulations

- PeleLM is a parallel, adaptive mesh refinement (AMR) code that solves the Navier-Stokes equations with in the low Mach number regime with the chemical reaction mechanisms.
- <https://amrex-combustion.github.io/PeleLM/overview.html>

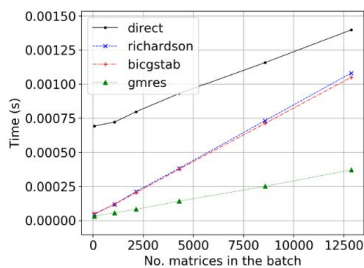


Problem	Size	Non-zeros (A)	Non-zeros (L+U)
dodecane_lu	54	2,332 (80%)	2,754 (94%)
drm19	22	438 (90%)	442 (91%)
gri12	33	978 (90%)	1,018 (93%)
gri30	54	2,560 (88%)	2,860 (98%)
isooctane	144	6,135 (30%)	20,307 (98%)
lidryer	10	91 (91%)	91 (91%)

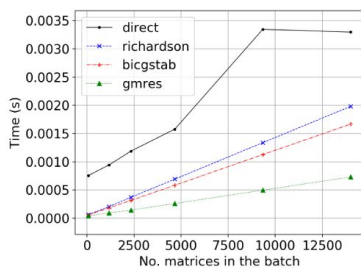
Application 3: Combustion simulations



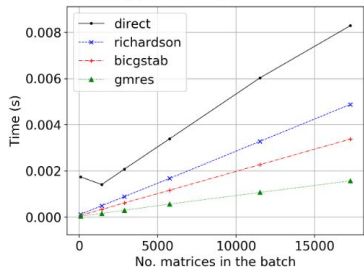
(a) dodecane_lu



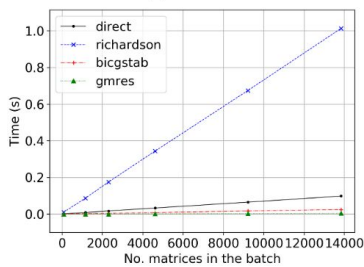
(b) drm19



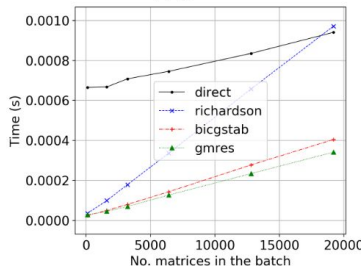
(c) gri12



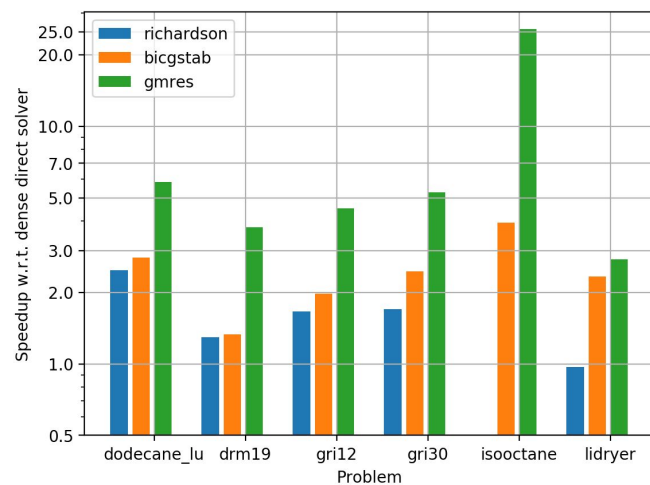
(d) gri30



(e) isoctane



(f) lidryer



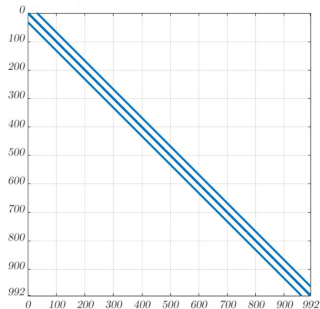
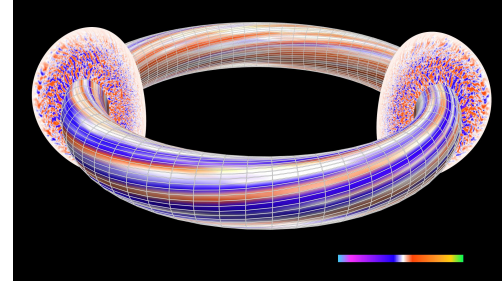
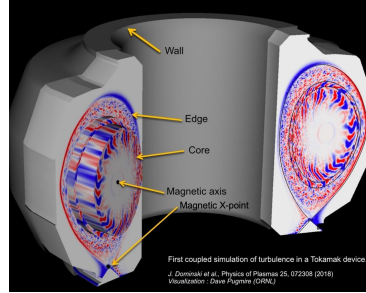
Speedups in production code may be larger:

- Use of "suitable" initial guess (last linear solve);
- Less accurate solution often sufficient;

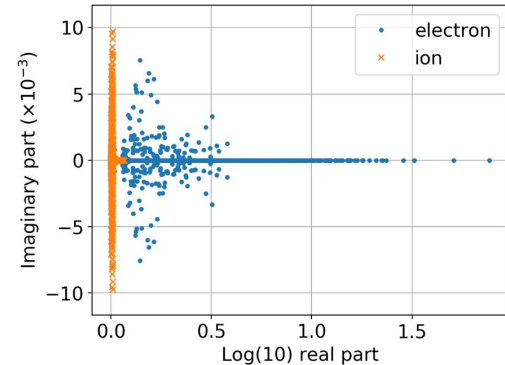
Application 4: Fusion plasma simulations

XGC is a gyrokinetic particle-in-cell code, which specializes in the simulation of the edge region of magnetically confined thermonuclear fusion plasma. The simulation domain can include the magnetic separatrix, magnetic axis and the biased material wall. *XGC* can run in total- δ - f , and conventional δ - f mode. The ion species are always gyrokinetic except for ETG simulation. Electrons can be adiabatic, massless fluid, drift-kinetic, or gyrokinetic.

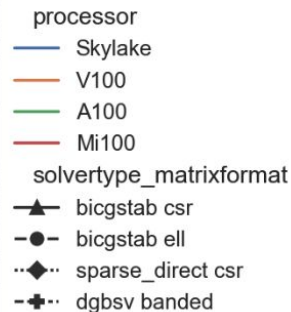
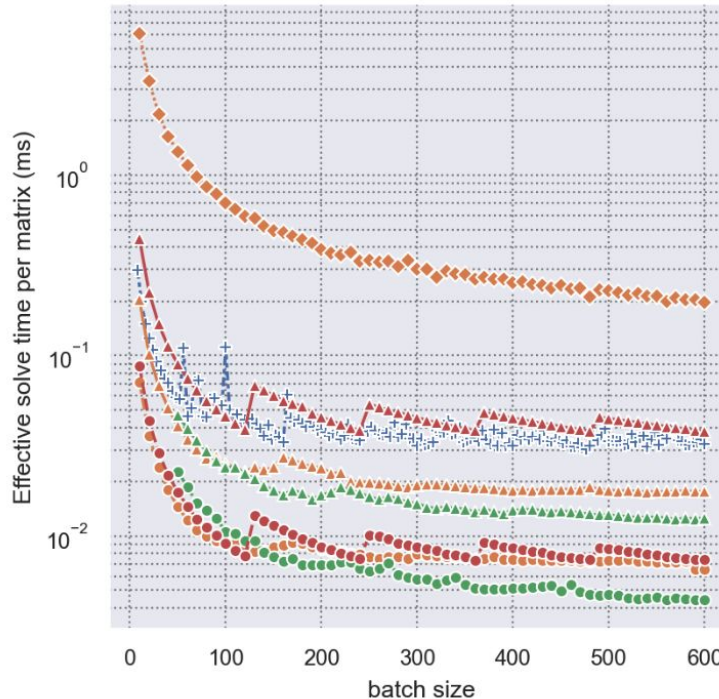
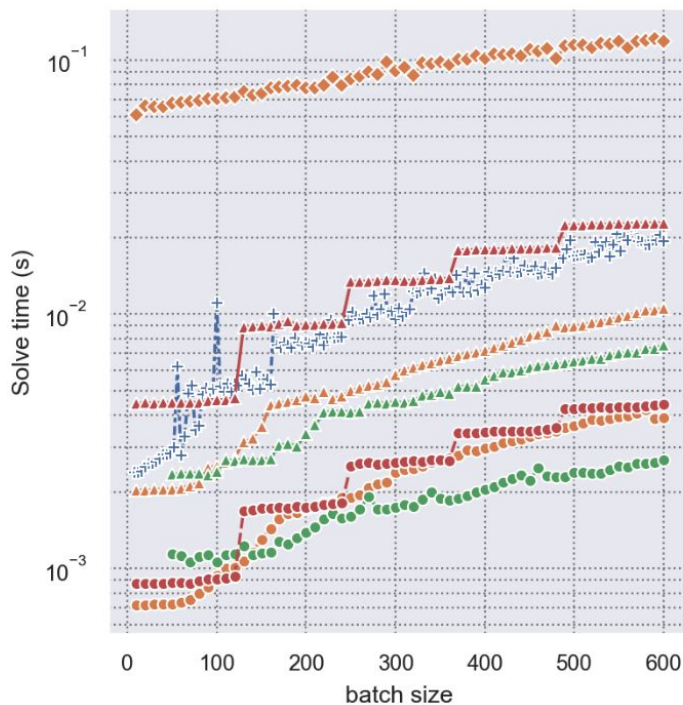
Source: https://xgc.pppl.gov/html/general_info.html



- Two species
- Ions easy to solve
- Electrons hard to solve
- Banded matrix structure
- Non-symmetric, need BiCGSTAB
- $n = \sim 1,000$
- $nz = \sim 9,000$



Application 4: Fusion plasma simulations



Batched Iterative solvers on GPUs for Fusion Plasma simulations, IPDPS 2022
Kashi, Nayak, Kulkarni, Lin and Anzt.

Outlook

- Efficient usage of GPUs is crucial in the path to Exascale.
- Ginkgo provides high performance implementations of many algorithms and we have shown good performance for a variety of applications.
- Distributed functionality in Ginkgo is bleeding edge, but has shown good scaling and performance.
- More mixed-precision functionality is being investigated (SpMV, solvers and preconditioners)
- A fully GPU enabled sparse direct solver will also be available soon in Ginkgo.

Thank you!
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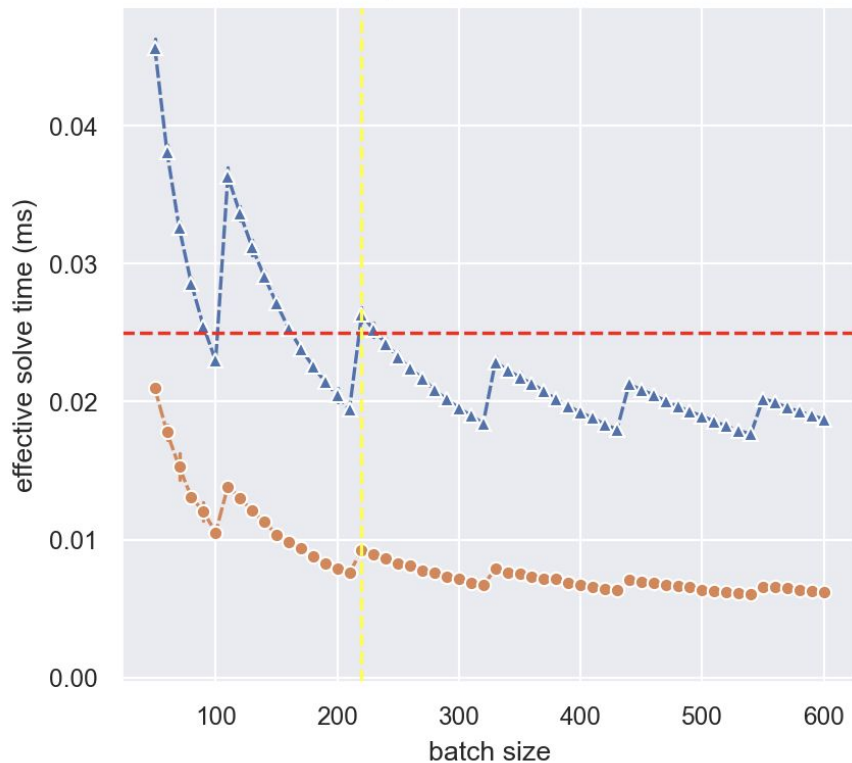


<https://github.com/ginkgo-project/ginkgo>

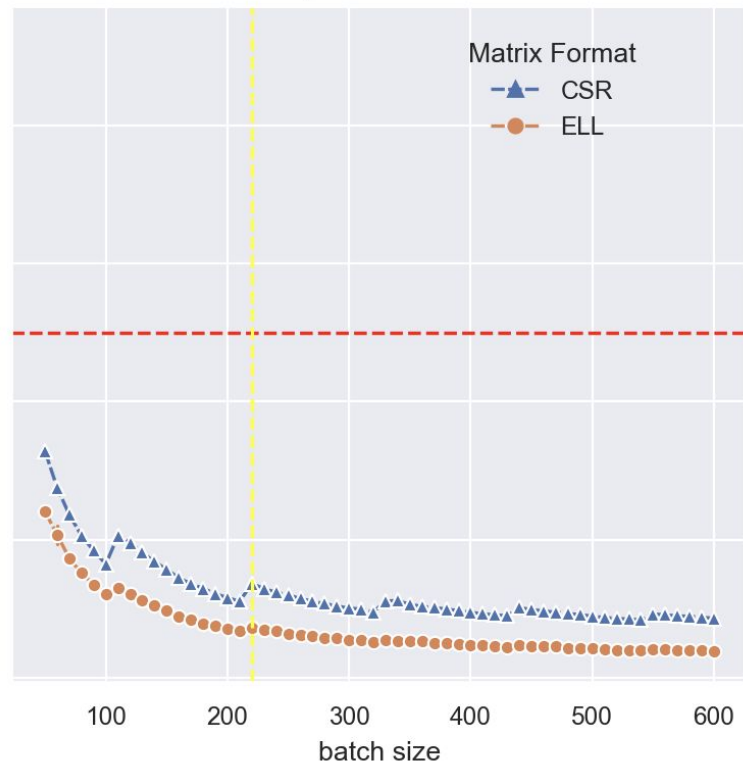
Bonus

Application 4: Fusion plasma simulations

species = electrons



species = ions



Application 1: Finite element library interfaces.

Example: Speeding up MFEM's "example 22" (damped harmonic oscillator) on NVIDIA and AMD GPUs

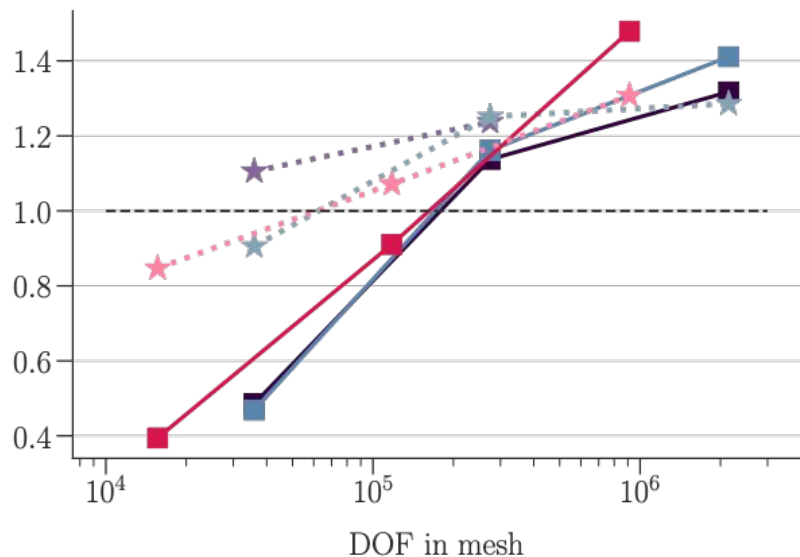
$$-\nabla \cdot (a \nabla u) - \omega^2 b u + i \omega c u = 0$$

$$a = 1, b = 1, \omega = 10, c = 20$$

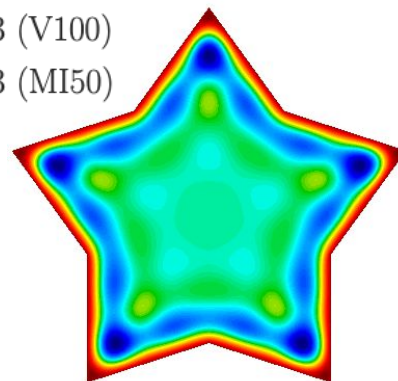


MFEM
Finite
element
library

Speedup for Ginkgo CB-GMRES vs MFEM

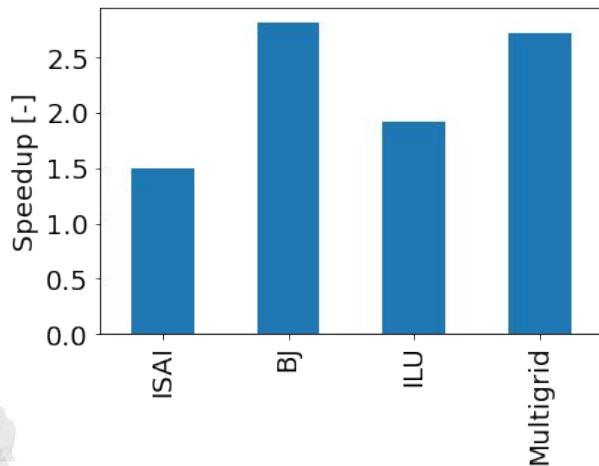
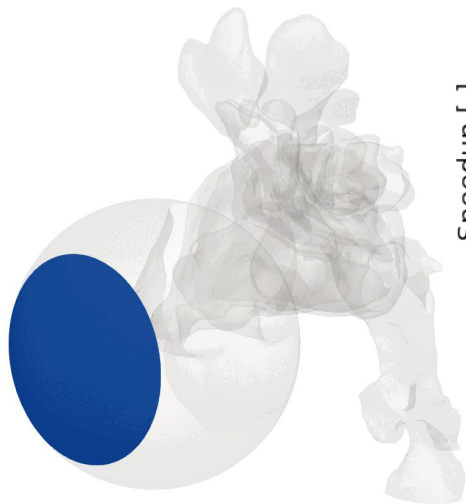


- p = 1 (V100)
- ★ p = 1 (MI50)
- p = 2 (V100)
- ★ p = 2 (MI50)
- p = 3 (V100)
- ★ p = 3 (MI50)

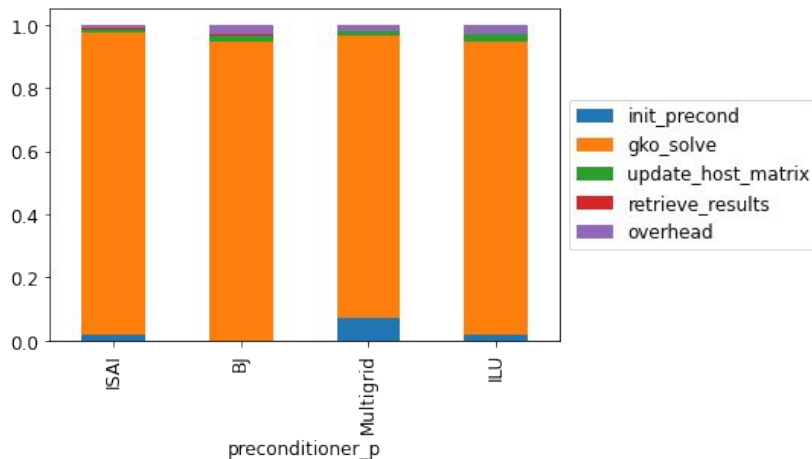


Application 2.3 : OpenFOAM (Nasal cavity)

OpenFOAM® +  Ginkgo = OGL¹



Total application speedup on one node with 4 GPUs



Solver cost breakdown

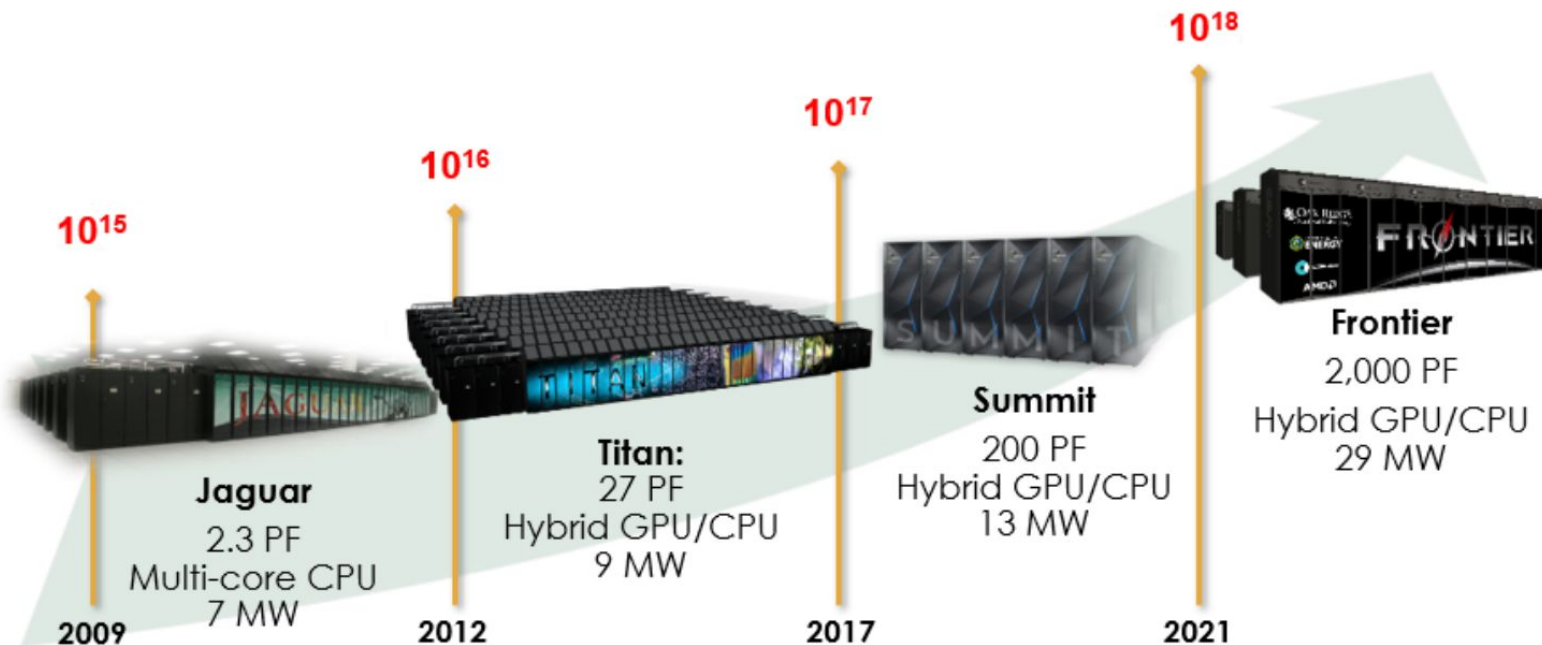
Airflow inside a human nose

¹Olenik,G: OGL: OpenFOAM Ginkgo layer: <https://github.com/hpsim/OGL>

The High Performance Computing (HPC) Landscape

System	Titan (2012)	Summit (2017)	Frontier (2021)
Peak	27 PF	200 PF	2 EF
# nodes	18,688	4,608	9,408
Node	1 AMD Opteron CPU 1 NVIDIA Kepler GPU	2 IBM POWER9™ CPUs 6 NVIDIA Volta GPUs	1 AMD EPYC CPU 4 AMD Radeon Instinct GPUs
Memory	0.6 PB DDR3 + 0.1 PB GDDR	2.4 PB DDR4 + 0.4 HBM + 7.4 PB On-node storage	4.6 PB DDR4 + 4.6 PB HBM2e + 36 PB On-node storage, 66 TB/s Read 62 TB/s Write
On-node interconnect	PCI Gen2 No coherence across the node	NVIDIA NVLINK Coherent memory across the node	AMD Infinity Fabric Coherent memory across the node
System Interconnect	Cray Gemini network 6.4 GB/s	Mellanox Dual-port EDR IB 25 GB/s	Four-port Slingshot network 100 GB/s
Topology	3D Torus	Non-blocking Fat Tree	Dragonfly
Storage	32 PB, 1 TB/s, <u>Lustre</u> Filesystem	250 PB, 2.5 TB/s, IBM Spectrum Scale™ with GPFS™	695 PB HDD+11 PB Flash Performance Tier, 9.4 TB/s and 10 PB Metadata Flash. <u>Lustre</u>
Power	9 MW	13 MW	29 MW

The High Performance Computing (HPC) Landscape



Read and writes significantly more expensive !

